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<b>6. AUTHOR(S)</b> Ratna Nandakumar				
<b>7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)</b> Department of Statistics University of Illinois 725 South Wright Street Champaign, IL 61820			<b>8. PERFORMING ORGANIZATION REPORT NUMBER</b>  1992 - No. 2	
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## ASSESSING ESSENTIAL DIMENSIONALITY-2

### Assessing Essential Dimensionality of Real Data

#### Abstract

The purpose of this article is to validate the capability of DIMTEST to assess essential dimensionality of the model underlying the item responses of real tests as opposed to simulated tests. A variety of real test data from different sources are used to assess essential dimensionality. Based on DIMTEST results, some test data are assessed as fitting an essential unidimensional model while others are not. Essential unidimensional test data, as assessed by DIMTEST, are then combined to form two-dimensional test data. The power of Stout's statistic T is examined for these two-dimensional data. It is shown that the results of DIMTEST on real tests replicate findings from simulated tests in that the statistic T discriminates well between essential unidimensional and multidimensional tests. It is also highly sensitive to major abilities while being insensitive to relatively minor abilities influencing item responses.

Subject terms: DIMTEST, essential independence, essential dimensionality, unidimensionality, multidimensionality, item response theory.

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Most of the currently used item response theory (IRT) models require the assumption of unidimensionality. From the strict IRT perspective, unidimensionality refers to one, and only one, trait underlying test items. Yet, it is a well known fact that items are multiply determined (Humphreys, 1981, 1985, 1986; Hambleton & Swaminathan, 1985, chap. 2; Reckase, 1979, 1985; Stout, 1987; Traub, 1983). Hence from the substantive viewpoint, the assumption of unidimensionality requires that the test items measure one dominant trait. Stout (1987) coined the term *essential unidimensionality* to refer to a particular mathematical formulation of a test having exactly one dominant trait. Dimensionality is, however, determined by the joint influence of test items and examinees taking the test (Reckase, 1990). In addition, extraneous factors such as teaching methods, anxiety level of examinees, etc., may also influence the dimensionality of the given item response data. Thus dimensionality has to be assessed each time a test is administered to a new group of examinees.

Factor analysis has traditionally been the most popular approach to assess dimensionality (Hambleton & Traub, 1973; Lumsden 1961). Factor analysis, despite its serious limitations to analyze dichotomous data (for example, see Hulin, Drasgow, and Parsons, 1983, chap. 8), has been the popular method to study the robustness of the unidimensionality assumption (Drasgow & Parsons 1983; Harrison, 1986; Reckase, 1979). There are a number of other promising methods proposed and used in varying degrees to assess dimensionality—to name a few: full information factor analysis based on the principle of marginal maximum likelihood (Bock, Gibbons, & Muraki, 1985; TESTFACT: Wilson, Wood, & Gibbons, 1983); nonlinear factor analysis (McDonald, 1962; McDonald & Ahlawat, 1974; Jamshid & McDonald, 1983); Holland and Rosenbaum's (1986) test of unidimensionality, monotonicity and conditional independence based on contingency tables; Tucker and Humphreys' methods based on the principle of local independence and second factor loadings (Roznowski, Tucker, & Humphreys, 1991); and Stout's (1987)

statistical procedure based on essential independence and essential dimensionality. Hattie (1984, 1985) has provided a comprehensive review of traditional approaches to assess dimensionality, and Zwick (1987) has applied some of the above mentioned recent procedures to assess dimensionality of National Assessment of Educational Progress data. Despite having several procedures available to assess dimensionality, there is no widespread consensus among substantive researchers for a preference for any method(s), and often there is dissatisfaction about assessing dimensionality (Berger & Knol, 1990; Hambleton & Rovinelli, 1986; Hattie, 1985).

Stout (1987) proposed a statistical test (DIMTEST) to assess essential unidimensionality of the latent space underlying a set of items. Nandakumar (1987) and Nandakumar and Stout (in press) have further modified, refined, and validated DIMTEST for assessing essential dimensionality on a variety of simulated tests. This article demonstrates the validity and usefulness of Stout's procedure on a variety of real, as opposed to simulated, tests. Test data from different sources are collected and used to assess essential unidimensionality. Essential unidimensional data are then combined to form two-dimensional data. The power of Stout's statistic  $T$  is examined for these two-dimensional data.

### DIMTEST for Assessing Essential Unidimensionality

DIMTEST, a statistical test for assessing unidimensionality, is based on the theory of essential dimensionality and essential independence (Stout, 1987, 1990). An item pool is said to be essentially independent with respect to the latent trait vector  $\Theta$  if, for a given initial segment of the item pool, the average absolute conditional (on  $\Theta$ ) covariances of item pairs approaches zero as the length of the segment increases. When only one dominant ability  $\Theta$  meets the essential independence assumption, the item pool is said to be

essentially unidimensional. In contrast, the assumption of local independence requires the conditional covariances to be zero for all item pairs in question. The number of abilities required to satisfy the local independence assumption is the dimensionality of the test. While the traditional definition of dimensionality (Lord & Novick, 1968) counts all abilities required to respond to test items correctly to satisfy the assumption of local independence, essential dimensionality counts only dominant abilities required to satisfy the assumption of essential independence (as opposed to local independence). DIMTEST, using this definition, assesses the closeness of approximation of the model generating the given item responses to the essential unidimensional model. Nandakumar (1991) describes the theoretical differences between traditional dimensionality and essential dimensionality and establishes through Monte Carlo studies the usefulness of DIMTEST for assessing essential unidimensionality in the possible presence of several secondary dimensions.

To use DIMTEST for assessing essential unidimensionality, it is assumed that a group of  $J$  examinees take an  $N$  item test. Each examinee produces a vector of responses of 1s and 0s, with 1 denoting a correct response and 0 denoting an incorrect response. It is assumed that essential independence with respect to some dominant ability  $\Theta$  holds and that the item response functions are monotonic with respect to the same vector  $\Theta$ . The hypothesis is stated as follows:

$$H_0 : d_E = 1 \text{ versus } H_1 : d_E > 1$$

where  $d_E$  denotes the essential dimensionality of the latent space underlying a set of items.

In order to assess essential unidimensionality of a given test data, DIMTEST follows several steps. The steps are summarized briefly here (for details see Stout 1987; Nandakumar & Stout, in press). First, test items are split into three subtests AT1, AT2, and PT with the aid of factor analysis (FA) using part of the sample (a sample size of 500

is recommended for this purpose). Items of AT1 are selected so that they all tap the same dominant ability. Instead of using FA, it is also possible to use expert opinion (EO) to select items for AT1. If the FA method of selection is chosen, DIMTEST automatically determines the length of the subtest AT1. Once items for AT1 are chosen, items of AT2 are selected so that they have a difficulty distribution similar to those of AT1 items (for details see Stout, 1987). The remaining items form the partitioning subtest PT.

Second, examinees are assigned to  $K$  different subgroups based on their score on the partitioning subtest PT. In other words, all examinees obtaining the same PT total score are assigned to the same subgroup. When the subtest PT is "long" and the test is essentially unidimensional, within each subgroup  $k$ , examinees are assumed to be approximately of similar ability. When PT is not long, the subtest AT2 compensates for the bias in AT1 caused by PT being short. Also, AT2 compensates for the bias in AT1 caused by the presence of guessing or the difficulty factor that is often found by the factor analysis.

Third, within each subgroup  $k$ , variance estimates,  $\hat{\sigma}_k^2$  and  $\hat{\sigma}_{U,k}^2$ , and the standard error of estimate  $S_k$  are computed using item responses of AT1. These estimates are then summed across  $K$  subgroups to obtain

$$T_L = \frac{1}{\sqrt{K}} \sum_{k=1}^K \left[ \frac{\hat{\sigma}_k^2 - \hat{\sigma}_{U,k}^2}{S_k} \right].$$

Similarly,  $T_B$  is computed using items of subtest AT2. Stout's statistic  $T$  is given by

$$T = (T_L - T_B) / \sqrt{2}.$$

The decision rule is to reject  $H_0$  if  $T \geq Z_\alpha$ , where  $Z_\alpha$  is the upper 100(1- $\alpha$ ) percentile of the

standard normal distribution,  $\alpha$  being the desired level of significance.

When the given test data are well modeled by an essential unidimensional model, items of AT1, AT2, and PT would all be tapping the same dominant dimension. Therefore, the variance estimates  $\hat{\sigma}_k^2$  and  $\hat{\sigma}_{U,k}^2$  will be approximately equal resulting in a "small"  $T$ -value, suggesting the tenability of  $H_0$ . On the other hand, when the test data is not well modeled by an essential unidimensional model, the variance estimate  $\hat{\sigma}_k^2$  will be much larger than  $\hat{\sigma}_{U,k}^2$  resulting in a "large"  $T$ -value leading to the rejection of  $H_0$ .

Simulation studies (Stout, 1987; Nandakumar, 1987; Nandakumar & Stout in press) on a wide variety of tests have demonstrated the utility of DIMTEST in discriminating between one- and two-dimensional tests. Simulation studies by Nandakumar (1991) have particularly demonstrated the usefulness of DIMTEST in assessing essential unidimensionality with the aid of a rough index of deviation from essential unidimensionality. The tests in Nandakumar (1991) were modeled by two- and higher-dimensional IRT models as opposed to a one-dimensional model, and the test items were influenced by major and secondary abilities to varying degrees. For some tests, the secondary ability or abilities influenced a high proportion of items, and for others the secondary ability or abilities influenced only a small proportion of items. It has been shown that DIMTEST reliably accepts the hypothesis of essential unidimensionality, provided the model generating the test is close to the essential unidimensional model: established when each of the secondary abilities influences relatively few items, or if secondary abilities are influencing many items, the degree of influence on each item is small. The type-I error in these cases was within tolerance of nominal level. As the degree of influence of the secondary abilities increases, however, the approximation to an essential unidimensional model degenerates, inflating the observed type-I error of the hypothesis of essential unidimensionality. Simulation results (Stout, 1987; Nandakumar and Stout, in press) have particularly demonstrated the excellent power of the statistic  $T$  when the model generating



the item responses is two-dimensional (two major abilities) with correlation between abilities as high as .7 and items jointly influenced by both abilities.

### Description of Data

The data sets used in the present study came from different sources. The U.S. history and literature data for grade 11/age 17, from the 1986 National Assessment of Educational Progress (NAEP, 1988) test data, were obtained from Educational Testing Service (ETS). The General Science data, Arithmetic Reasoning data, and Auto Shop Information data for grades 10 and 12, from the Armed Services Vocational and Aptitude Battery (ASVAB) test data, were obtained from Linn, Hastings, Hu, and Ryan (1987). The Mathematics Usage test data, the science test data, and the reading test data were obtained from American College Testing program (ACT).

The NAEP achievement tests are part of the so called Balanced Incomplete Block (BIB) design with spiraled administration (Rogers et al., 1988) which allows the study of interrelationships among all items within a subject area. Because the U.S. history and literature tests fall into the simplest category of BIB design, it was relatively easy to gather the response data for all examinees taking these tests. Hence, these tests were chosen for the present study. The items in each area (history and literature) were divided into four "parallel" blocks with approximately the same number of items. One block of items out of four was randomly selected in each case for the present study.

The U.S. history test data (HIST-A) with 36 items consists of items requiring knowledge from different time periods of U.S. history: Colonization to 1763; the Revolutionary War and the New Republic, 1763-1815; Civil War, 1815-1877; the rise of modern America, World War I 1877-1920; the Depression, World War II, 1920-1945; Post-World War II, 1945-to the present; and map items requiring the knowledge of

geographical location of different countries in the world. A 31-item subtest of HIST-A, named HIST was created (explained in detail in the next section) consisting of all the items of HIST-A, except the five map items. There are 2428 examinees in the HIST-A and HIST samples.

The literature test data (LIT) with 30 items consists of items requiring knowledge within four literary genres: novels, short stories, and plays; myths, epics, and Biblical characters and stories; poetry; and nonfiction. There are 2439 examinees in the LIT sample.

The ASVAB tests are used by the Department of Defense Student Testing Program in high schools and post secondary schools. The Arithmetic Reasoning test data for grades 10 and 12, with 30 items each, consists of items requiring knowledge in solving arithmetic word problems. The arithmetic reasoning test sample for grade 10 (AR10) has 1984 examinees, and for grade 12 (AR12) has 1961 examinees. The Auto and Shop Information test data for grades 10 and 12, with 25 items, each consists of items requiring knowledge of automobile, tools, and shop terminology and practices. The auto shop test sample for grade 10 (AS10) has 1981 examinees, and for grade 12 (AS12) has 1974 examinees. The General Science test data for grades 10 and 12, with 25 items each, consists of items requiring knowledge in solving high school level physical, life, and earth sciences. There are 1990 examinees in the general science test sample for grade 10 (GS10) and 1990 examinees in the general science grade 12 (GS12) sample.

The ACT mathematics usage test data (MATH) with 40 items consists of items requiring knowledge in solving different types of mathematics problems: arithmetic and algebra operations, geometry, numeration, story problems, and advanced topics. There are 2491 examinees in the MATH sample.

The ACT reading test data (READ-A) with 40 items consists of 4 passages, each followed by 10 questions. The first three passages are taken from different books all dealing with humanities, and the last passage is taken from a book about psychology. The first

passage came from Of the Farm by John Updike. The second passage came from Light and Color in Nature and Art by Samuel Williamson and Herman Cummins. The third passage came from Theatre: the Dynamics of the Art by Brian Hansen. And the fourth passage came from Toward a Psychology of Being by Abraham Maslow. A 30-item subset of READ-A named READ was created (details in the next section) consisting of the first 30 items of READ-A. There are 5000 examinees in the READ-A and READ samples.

The ACT science test data (SCI-A) with 40 items consists of 7 passages, each followed by 5 to 7 questions. The first passage dealt with the effect of the thymus gland on the development of immune system in mice. The second passage dealt with sub-surface ground water movement and its effects for waste disposal. The third passage dealt with the periods of the pendulum on the earth and the moon and its relationship to the string length and mass of the ball. The fourth passage dealt with the environmental impact of effluent. The fifth passage dealt with a bimetallic catalyst and its relationship to the speed of certain chemical reactions. The sixth passage dealt with the views of two paleontologists on the characteristics of dinosaurs. And the seventh passage dealt with the principals of osmosis and osmotic characteristics of 3 categories of organisms. A 28-item subset of SCI-A named SCI was created (explained in the next section) consisting of the first 28 items of SCI-A. There are 5000 examinees in SCI-A and SCI samples.

In addition, in order to examine the effect of sample size on DIMTEST, both SCI and READ are randomly split into four mutually exclusive data sets. The READ is split into READ1, READ2, READ3, and READ4—with 750, 1000, 1250 and 2000 examinees, respectively. Similarly SCI is split into SCI1, SCI2, SCI3, and SCI4—with 750, 1000, 1250, and 2000 examinees, respectively. In all there are 22 test data. These are listed along with the test size and sample size in the first three columns of Tables 1 and 2.

### Creation of Two-Dimensional Test Data

Three different sets of two-dimensional test data from the content perspective were created by combining responses from test data that were assessed as essentially unidimensional by DIMTEST in the present study.

The two-dimensional test data, RS, was created by combining responses of 30 items of READ with the responses of 6 items of SCI forming a 36-item test with 5000 examinees. The 6 items of SCI are part of one of the passages randomly selected from its 5 passages. Just as in the unidimensional case of READ and SCI, RS is then randomly split into 4 mutually exclusive data sets RS1, RS2, RS3, and RS4—with 750, 1000, 1250 and 2000 examinees, respectively. These tests are listed along with their test sizes and sample sizes in the first four columns of Table 3.

The two-dimensional test data ARGS1, for Grade 10, was created by combining the responses of 30 items from AR10 with the responses of 5 items (randomly selected from 25 item responses) from GS10. Similarly, ARGS2 was created by combining the responses of 30 items from AR10 with the responses of 10 items from GS10. The two-dimensional test data GSAR1, for grade12, was created by combining the responses of 25 items from GS12 with the responses of 5 items from AR12; and GSAR2 was created by combining the responses of 25 items from GS12 with responses of 10 items from AR12. These test data are listed along with their test sizes and sample sizes in the first four columns of Table 4.

The two-dimensional test data HSTLIT1 was created by combining the responses of 31 items from HIST with the responses of 5 items (randomly selected from 30 item responses) from LIT. Similarly HSTLIT2 and HSTLIT3 were created by combining the responses of 31 items from HIST with the responses of 8 and 10 items, randomly selected, from LIT respectively. These test data are listed along with their test sizes and sample sizes in the first four columns of Table 5.

## Results

### Unidimensional Studies

All the tests in Table 1, except HIST, READ, and SCI (which are derived subtests of HIST-A, READ-A, and SCI-A, respectively as described below), were initially tested for essential unidimensionality using DIMTEST. In each case, 500 examinees were randomly selected from the given pool for the use of selecting AT1 items, using factor analysis. The rest of the items were used for computing Stout's statistic  $T$ . The size of AT1 ( $M$ ) was also determined by DIMTEST. For each test, the  $T$ -value and the  $p$ -value are noted. Table 1 lists the  $T$ - and  $p$ -values for all tests in the fourth and fifth columns. The method of selection of the AT1 subtest, the value of  $M$ , and item numbers selected for AT1 are listed in the last three columns of Table 1.

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Table 1 about here

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It can be seen from Table 1 that the  $p$ -values associated with test data LIT, AR10, AR12, GS10, and GS12 are well above the nominal level of significance ( $\alpha=.05$ ), thereby strongly affirming essential unidimensional nature of these tests. That is, the underlying model generating the test data is judged essentially unidimensional. However, the  $p$ -values associated with HIST-A, AS10, AS12, MATH, READ-A, and SCI-A are well below the nominal level of significance of .05, thereby strongly affirming the multidimensional nature of these test data. For these tests where  $p$ -values were below the nominal level, the nature of multidimensionality was further explored.

When the test data are essentially unidimensional, items of AT1 are, by logic, of the same dominant dimension as the rest of the items; therefore, DIMTEST does not reject the null hypothesis. When the test data is not unidimensional, however, the items of AT1 are dimensionally different from the rest of the items, and DIMTEST rejects the null hypothesis of essential unidimensionality. Following this reasoning for tests where  $p$ -values were very low, the content of items of AT1 were examined. Table 1 shows that for HIST-A, items 12 through 16 and item 6 were selected for AT1. Upon studying the content of these items, it was found that items 12 through 16 were homogeneous and differed dimensionally from the rest of the items of HIST-A; these 5 items require the knowledge of location of different countries on the world map (map items), while the rest of the items deal with U.S. history. It is also possible in theory that these items were selected for AT1 due to chance alone. In order to test for this, DIMTEST was applied on the given sample of 2428 examinees 100 times repeatedly, each time randomly splitting 2428 examinees into two groups of 500 and 1928 examinees. That is, AT1 items were selected repeatedly on different random samples of 500 examinees each. The resampling results showed that items 12 through 16 were consistently selected for AT1. In addition to these items one or two more items, which varied from run to run, were selected from the rest of the items. Hence it was concluded that the map items are dimensionally different from the rest. A subset HIST was formed consisting of all items of HIST-A except for map items. It can be seen from Table 1 that the  $p$ -value associated with HIST ( $p=.095$ ) shows evidence of essential unidimensionality. Furthermore, from the content perspective, items of AT1 do not form a set that is dimensionally different from the rest of the items of HIST.

A similar phenomenon was observed with test data READ-A and SCI-A. For READ-A, the last 10 items (items followed by the last passage) formed part of subtest AT1. Again these same 10 items formed part of AT1 in repeated resampling applications of DIMTEST. Upon studying the content of these items, it was found that these 10 items

tapped "psychology" content area which is different from the "literature," tapped by the first three passages. Another possibility is that, since these are the last 10 items of reading test, speededness could have caused the secondary dimension. Based on these observations, it was concluded that these items were dimensionally different from the rest, and a subset READ was formed consisting of first 30 items of READ-A. It can be seen from Table 1 that the  $p$ -value associated with READ ( $p=.32$ ) shows strong evidence of an essential unidimensional model underlying the test items. In addition, items of AT1 now come from all the passages of READ.

For test data SCI-A, the 12 items following the last two passages formed part of AT1. Just as in HIST-A and READ-A, after resampling application of DIMTEST, these items were removed. The resulting subtest SCI with the first 28 items was still found to be multidimensional ( $p=.002$ ). Thus, a unidimensional subset could not be formed. Unlike reading test items, science test items come from distinctly different content areas, with a moderate correlation among content areas, and require a higher level of abstract reasoning and analytical skills than the reading items. Thus, in addition to content areas, difficulty or speededness could have caused major secondary dimensions in this case.

For the test data MATH, AS10, and AS12, where  $p$ -values were low, items of AT1 did not form a subgroup tapping a secondary ability as found in HIST-A, READ-A, or SCI-A. In addition upon studying the content of the items, it was found these items tap multiple major content areas. Therefore these test data are treated as multidimensional.

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Table 2 about here

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Table 2 shows dimensionality results of the unidimensional READ and

multidimensional SCI test data for different sample sizes. The  $p$ -values associated with READ1 through READ4 show evidence of a high degree of essential unidimensionality underlying the test data. These results are consistent with that of READ in Table 1. The selection of items of AT1 for tests READ1 through READ4 are highly varied, and yet they consistently affirm essential unidimensionality. The results of SCI1 through SCI4 are consistent with that of SCI in Table 1 in affirming multidimensionality of the test data. Items of AT1 varied highly for all four tests and yet consistently affirmed multidimensionality, except for SCI3.

### Two-dimensional Studies

Results of two-dimensional reading and science test data are reported in Table 3. Since items that tap a distinct second dimension, from the content perspective, are clearly known (in this case, 6 SCI items), the science items were forced to be selected for AT1. This is an example where expert opinion is used to select AT1 items. The  $T$ - and  $p$ -values for RS1, RS2, RS3, RS4, and RS strongly confirm the two-dimensional nature of these test data. As expected, as the sample size increases, the power also increases.

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Table 3, Table 4 and Table 5 about here

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The results of the two-dimensional test data of ARGs and GSAR are reported in Table 4. Also in this case, since items that are used to create these two-dimensional data are known (GS items for ARGs and AR items for GSAR), these items were forced to be selected for AT1. The  $T$ - and  $p$ -values associated with all the four tests strongly confirm



the multidimensionality of these test data. For ARGS1 and ARGS2, there is a sharp increase in  $T$ - and  $p$ -values as the degree of contamination, as measured by the number of item responses contaminated, increases from 5 to 10.

The results of the two-dimensional history and literature test data are reported in Table 5. As with other two-dimensional tests, LIT items were forced to be selected for AT1. Also in this case, the  $T$ - and  $p$ -values confirm the multidimensional nature of these data.

DIMTEST was again applied to a sample of test data selected from two-dimensional tests. This time FA was used as the method of selection for AT1 items. The purpose of this analysis was to check if the FA method of selection of AT1 items would lead to the similar  $p$ -values as with EO. The findings revealed that for these tests FA could not always ferret out purely unidimensional items from content perspective. The subtest AT1 had a mixture of items tapping both dimensions, and DIMTEST was then able to correctly assess dimensionality only when there were 1000 or more examinees for computing the statistic.

### Discussion and Conclusions

None of the tests examined in the present study are strictly unidimensional in the sense of measuring only one ability. Items, in every test, are influenced by several secondary abilities in addition to the major ability intended to be measured. Based on DIMTEST analysis, some test data were assessed as fitting an essential unidimensional model while others were not. This depends upon whether the secondary abilities were major or minor.

The unidimensionality analysis of HIST-A, READ-A, and SCI-A present interesting findings. For HIST-A, the map items had high second factor loadings and thus were selected for AT1. Consequently, the computed  $T$ -statistic was large, leading to the

rejection of  $H_0$  and implying that AT1 items are dimensionally different from the rest of the test. Content analysis of HIST-A reveals that HIST-A consists of items of United States history for different time periods spanning from 1763 to present time. These items cover such a large span of time that the test is surely slightly multidimensional for this reason alone. In addition, the test contains map items. The map items, however, were isolated and statistically confirmed as not measuring the same trait as the rest of the test. This shows that the statistic  $T$  is highly sensitive to distinct major dimensions (in this case, map items). The analysis of HIST, with map items removed, reveals that it is essentially unidimensional. Thus the statistic  $T$  seems to be robust against relatively minor correlated abilities influencing test items while being sensitive to major abilities. Likewise, for the test data READ-A, multidimensionality was caused by items tapping psychology topic (scientific) versus literature topics (humanities). Once the psychology item responses were removed, the remaining item responses could be well modeled by an essential unidimensional model. In contrast, the multidimensionality in SCI-A was due to not only distinct major abilities but also likely due to speededness of the test, which in itself is a major determinant. Moreover, an essential unidimensional subtest could not be formed for SCI-A.

Another interesting feature of these analyses is that although both READ and SCI are paragraph comprehension type test data, they differ widely in the degree of their approximation to essential dimensionality. The READ test data has 3 passages each followed by 10 items, all dealing with humanities. Although these passages come from different sources, the model underlying the item responses approximates an essential unidimensional model. This is an example where a few secondary abilities (possibly highly correlated) each influence a large group of items. In contrast, the SCI test data has 5 passages each followed by 5 or 6 items. These passages, although they deal with science in general, come from widely different and conceptually difficult topics, and the model

underlying the item responses does not approximate an essential unidimensional model. This is an example where many secondary abilities each influence a small groups of items, but the strength of the influence of these secondary abilities is such that item responses can not be well modeled by an essential unidimensional model. These results are consistent with simulation results of Nandakumar (1991) in that the number of items influenced by secondary abilities and the strength of the secondary abilities present determine the degree to which the assumption of essential unidimensionality is violated.

The results obtained in this study are similar to the results obtained by other researchers who have analyzed some of these data using different statistical methodologies. Zwick (1987) performed dimensionality analyses of HIST-A and LIT by various techniques to assess dimensionality and concluded that these are unidimensional. Regarding the ACT data, it is believed that MATH and SCI are multidimensional. Bock, Gibbons, and Muraki (1985) have analyzed ASVAB test data for a different sample and found a significant second factor for arithmetic reasoning, general science, and auto shop information. Since the sample used here is not the same it is hard to develop a meaningful comparison.

The results of two-dimensional tests demonstrate a very good power of the statistic  $T$ . The statistic  $T$  has the capability to ignore minor secondary traits, which should be largely discounted, from the major dominant traits. This is evidenced in several cases. The test data HIST illustrates this. There is inherent multidimensionality in HIST as it covers a range of time periods in history. However, the  $p$ -value is above the nominal level of significance, suggesting acceptance of unidimensionality. By contrast, with the additional contamination of only 5 LIT items or 5 map items, the  $T$ -value shoots up, indicating essential multidimensionality of the data. This remarkable sensitivity of the statistic  $T$  to major dimensions illustrates its power.

These results, for the first time, have illustrated both the factor analysis approach and the expert opinion approach to select items for the subtest AT1. Tables 1 and 2 use FA

to select AT1 items, and Tables 3, 4, and 5 use EO. It is evident that FA serves as an exploratory tool and EO serves as a confirmatory tool in selecting items for AT1 to assess essential dimensionality.

The dimensionality of a given set of item responses in certain sense is a continuum—one cannot determine whether a given data of responses generated by a set of items to an examinee sample is truly essentially unidimensional or truly multidimensional; one can only approximate. Although the exact number of dimensions in an IRT model is rigorously defined for a finite length test, the number of dominant dimensions—whether determined by Stout's essential dimensionality conceptualization or by some other conceptualization—is only rigorously definable for an infinitely long test. In other words, for a finite test (that is, for any real test data) it is a judgment call whether a particular IRT model is seen as having one, or more than one, dominant dimension, based upon where on the continuum the amount of multidimensionality falls. One consequence of this is that the performance of ability estimation procedures such as LOGIST or BILOG needs to be addressed in the context of the assessment of the amount of lack of unidimensionality. In this regard, indices of lack of essential unidimensionality developed by Junker and Stout (1991) will be extremely useful. These indices can be used to decide when it is safe to use unidimensional estimation procedures such as LOGIST and BILOG to arrive at accurate estimates of ability.

In cases where approximation of essential unidimensional model to the data is in question, there are various alternatives. The test items can be split into essential unidimensional subtests (for example, HIST-A and READ-A). Another possible approach is to investigate the applicability of the concept of "testlet" to the data (Rosenbaum, 1988; Thissen, Steinberg, and Mooney, 1989). If the assumption of local independence is violated within the passages but maintained among the passages, the theory of testlets promises unidimensional scoring for such tests. The test data SCI-A and SCI could fall into this

category. Multidimensional modeling can be applied if either of the above procedures can not be applied (Reckase, 1989).

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Table 1  
Results of  $H_0: d_E = 1, \alpha = .05$

Test	No. of items	No. of Examinees	T	p	Selection of AT1 items	M**	Items of AT1
HIST-A	36	2428	6.19	.00001	FA	6	6,12,13,14,15,16
HIST	31	2428	1.31	.095	FA	5	7,23,24,26,30
LIT	30	2439	.71	.234	FA	6	5,9,18,20,22,26
AR10	30	1984	-.75	.727	FA	6	1,3,4,5,6,8
AR12	30	1961	.64	.260	FA	4	1,4,6,14
GS10	25	1990	.96	.168	FA	5	4,16,19,23,25
GS12	25	1988	-.26	.601	FA	6	14,15,19,23,24,25
AS10	25	1981	2.27	.012	FA	5	4,16,19,23,25
AS12	25	1974	3.64	.000	FA	5	3,4,8,14,22
MATH	40	2491	2.79	.003	FA	10	1,5,25,27,29,30 32,34,35,39
READ-A	40	5000	8.67	.00001	FA	10	31,32,33,34,35,36, 37,38,39,40
READ	30	5000	.48	.32	FA	7	1,2,6,11,12,13,21
SCI-A	40	5000	3.19	.0007	FA	12	29,30,31,32,33,34 35,36,37,38,39,40
SCI	28	5000	2.97	.002	FA	5	2,3,5,8,12

\* AT1 items can be selected by using factor analysis (FA) or by expert opinion (EO).

\*\* M is the size of AT1

Table 2  
Results of  $H_0: d_E = 1, \alpha = .05$

Test	No. of items	No. of examinees	T	p	Selection of AT1 items	M	Items of AT1
READ1	30	750	.05	.480	FA	5	11,12,13,15,17
READ2	30	1000	.48	.317	FA	7	1,2,6,11,12,13,21
READ3	30	1250	-.06	.524	FA	7	2,4,6,9,11,12,13
READ4	30	2000	1.01	.155	FA	5	1,11,12,13,16
SCI1	28	750	1.89	.029	FA	7	1,3,4,5,17,20,21
SCI2	28	1000	3.19	.007	FA	6	8,12,14,18,20,24
SCI3	28	1250	1.38	.080	FA	7	6,9,10,11,19,25,28
SCI4	28	2000	2.91	.001	FA	7	8,9,10,11,12,19,22

Table 3  
Results of  $H_0: d_E = 1$  for two-dimensional tests:  
READ & SCI;  $\alpha = .05$

Test	No. of Items		No. of Examinees	$T$	$p$	Selection of AT1 items	$M$	Items of AT1
	RAED	SCI						
RS1	30	6	750	1.92	.020	E0	6	31,32,33,34,35,36
RS2	30	6	1000	2.72	.003	E0	6	31,32,33,34,35,36
RS3	30	6	1250	3.71	.0001	E0	6	31,32,33,34,35,36
RS4	30	6	2000	3.32	.0005	E0	6	31,32,33,34,35,36
RS	30	6	5000	6.83	.0000	E0	6	31,32,33,34,35,36

Table 4  
Results of  $H_0: d_E = 1$  for two-dimensional tests:  
AR & GS;  $\alpha = .05$

Test	No. of Items		No. of Examinees	$T$	$p$	Selection of AT1 items	$M$	Items of AT1
	AR	GS						
ARGS1	30	5	1853	2.85	.002	E0	5	31,32,33,34,35
ARGS2	30	10	1853	6.15	.000	E0	10	31,32,33,34,35, 36,37,38,39,40
GSAR1	25	5	1811	4.29	.000	E0	5	26,27,28,29,30
GSAR2	25	10	1811	4.06	.000	E0	10	26,27,28,29,30, 31,32,33,34,35

Table 5  
Results of  $H_0: d_E = 1$  for two-dimensional tests:  
HIST & LIT;  $\alpha = .05$

Test	No. of Items		No. of Examinees	$T$	$p$	Selection of AT1 items	$M$	Items of AT1
	HIST	LIT						
HSTLIT1	31	5	2428	3.01	.036	E0	5	32,33,34,35,36
HSTLIT2	31	8	2428	3.38	.000	E0	8	32,33,34,35,36, 37,38,39
HSTLIT3	31	10	2428	2.03	.021	E0	10	32,33,34,35,36, 37,38,39,40,41

Dr. Terry Ackerman  
Educational Psychology  
260C Education Bldg.  
University of Illinois  
Champaign, IL 61801

Dr. Terry Allard  
Code 1142CS  
Office of Naval Research  
810 N. Quincy St.  
Arlington, VA 22217-5000

Dr. Nancy Allen  
Educational Testing Service  
Princeton, NJ 08541

Dr. Gregory Anrig  
Educational Testing Service  
Princeton, NJ 08541

Dr. Phippe Arabia  
Graduate School of Management  
Rutgers University  
42 New Street  
Newark, NJ 07102-1895

Dr. Isaac I. Bejar  
Law School Admissions  
Services  
Box 40  
Newtown, PA 18940-0040

Dr. William O. Berry  
Director of Life and  
Environmental Sciences  
AFOSR/NL, N1, Bldg. 410  
Rolling AFB, DC 20332-6448

Dr. Thomas G. Bever  
Department of Psychology  
University of Rochester  
River Station  
Rochester, NY 14627

Dr. Menucha Birenbaum  
Educational Testing  
Service  
Princeton, NJ 08541

Dr. Bruce Blossom  
Defense Manpower Data Center  
94 Pacific St.  
Suite 155A  
Monterey, CA 93943-3231

Dr. Gwyneth Boodoo  
Educational Testing Service  
Princeton, NJ 08541

Dr. Richard L. Branch  
HQ, USMEPCOM/MEPCT  
2510 Green Bay Road  
North Chicago, IL 60064

Dr. Robert Brennan  
American College Testing  
Programs  
P. O. Box 168  
Iowa City, IA 52243

Dr. David V. Budescu  
Department of Psychology  
University of Haifa  
Mount Carmel, Haifa 31999  
ISRAEL

Dr. Gregory Candell  
CTB/MacMillan/McGraw-Hill  
2518 Garden Road  
Monterey, CA 93940

Dr. Paul R. Chatelier  
Perceptronics  
1911 North Ft. Myer Dr.  
Suite 1100  
Arlington, VA 22209

Dr. Susan Chipman  
Cognitive Science Program  
Office of Naval Research  
800 North Quincy St.  
Arlington, VA 22217-5000

Dr. Raymond E. Christal  
UES LAMP Science Advisor  
AL/HRMIL  
Brooks AFB, TX 78235

Dr. Norman Cliff  
Department of Psychology  
Univ. of So. California  
Los Angeles, CA 90089-1061

Director  
Life Sciences, Code 1142  
Office of Naval Research  
Arlington, VA 22217-5000

Commanding Officer  
Naval Research Laboratory  
Code 4827  
Washington, DC 20375-5000

Dr. John M. Cornwell  
Department of Psychology  
IO Psychology Program  
Tulane University  
New Orleans, LA 70118

Dr. William Crano  
Department of Psychology  
Texas A&M University  
College Station, TX 77843

Dr. Linda Curran  
Defense Manpower Data Center  
Suite 400  
1600 Wilson Blvd  
Rosslyn, VA 22209

Dr. Timothy Davey  
American College Testing Program  
P.O. Box 168  
Iowa City, IA 52243

Dr. Charles E. Davis  
Educational Testing Service  
Mail Stop 22-T  
Princeton, NJ 08541

Dr. Ralph J. DeAyala  
Measurement, Statistics,  
and Evaluation  
Benjamin Bldg., Rm. 1230F  
University of Maryland  
College Park, MD 20742

Dr. Sharon Derry  
Florida State University  
Department of Psychology  
Tallahassee, FL 32306

Hei-Ki Dong  
Bellcore  
6 Corporate Pl.  
RM: PYA-1K207  
P.O. Box 1320  
Piscataway, NJ 08855-1320

Dr. Neil Dorans  
Educational Testing Service  
Princeton, NJ 08541

Dr. Fritz Drasgow  
University of Illinois  
Department of Psychology  
603 E. Daniel St.  
Champaign, IL 61820

Defense Technical  
Information Center  
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Dr. Richard Duran  
Graduate School of Education  
University of California  
Santa Barbara, CA 93106

Dr. Susan Embretson  
University of Kansas  
Psychology Department  
426 Fraser  
Lawrence, KS 66045

Dr. George Engethard, Jr.  
Division of Educational Studies  
Emory University  
210 Fishburne Bldg.  
Atlanta, GA 30322

ERIC Facility-Acquisitions  
2440 Research Blvd., Suite 550  
Rockville, MD 20850-3238

Dr. Marshall J. Farr  
Farr-Sight Co.  
2520 North Vernon Street  
Arlington, VA 22207

Dr. Leonard Feldt  
Lindquist Center  
for Measurement  
University of Iowa  
Iowa City, IA 52242

Dr. Richard L. Ferguson  
American College Testing  
P.O. Box 168  
Iowa City, IA 52243

Dr. Gerbard Fischer  
Liebiggasse 5  
A 1010 Vienna  
AUSTRIA

Dr. Myron Fischl  
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DAPE-HR  
The Pentagon  
Washington, DC 20310-0300

Mr. Paul Foley  
Navy Personnel R&D Center  
San Diego, CA 92152-6800

Chair, Department of  
Computer Science  
George Mason University  
Fairfax, VA 22030

Dr. Robert D. Gibbons  
University of Illinois at Chicago  
NP1 909A, M/C 913  
912 South Wood Street  
Chicago, IL 60612

Dr. Janice Gifford  
University of Massachusetts  
School of Education  
Amherst, MA 01003

Dr. Robert Glaser  
Learning Research  
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University of Pittsburgh  
3939 O'Hara Street  
Pittsburgh, PA 15260

Dr. Susan R. Goldman  
Peabody College, Box 45  
Vanderbilt University  
Nashville, TN 37203

Dr. Timothy Goldsmith  
Department of Psychology  
University of New Mexico  
Albuquerque, NM 87131

Dr. Sherrin Gou  
AFHRL/MOMJ  
Brooks AFB, TX 78235-5601

Dr. Bert Green  
Johns Hopkins University  
Department of Psychology  
Charles & 34th Street  
Baltimore, MD 21218

Prof. Edward Haertel  
School of Education  
Stanford University  
Stanford, CA 94305-3096

Dr. Ronald K. Hambleton  
University of Massachusetts  
Laboratory of Psychometric  
and Evaluative Research  
Hills South, Room 152  
Amherst, MA 01003

Dr. Delwyn Hamisch  
University of Illinois  
51 Gerry Drive  
Champaign, IL 61820

Dr. Patrick R. Harrison  
Computer Science Department  
U.S. Naval Academy  
Annapolis, MD 21402-5002

Ms. Rebecca Hettler  
Navy Personnel R&D Center  
Code 13  
San Diego, CA 92152-6800

Dr. Thomas M. Hirsch  
ACT  
P. O. Box 168  
Iowa City, IA 52243

Dr. Paul W. Holland  
Educational Testing Service, 21-T  
Rosedale Road  
Princeton, NJ 08541

Prof. Lutz F. Hornke  
Institut für Psychologie  
RWTH Aachen  
Jaegersstrasse 17/19  
D-4100 Aachen  
WEST GERMANY

Ms. Julia S. Hough  
Cambridge University Press  
40 West 20th Street  
New York, NY 10011

Dr. William Howell  
Chief Scientist  
AFHRL/CA  
Brooks AFB, TX 78235-5601

Dr. Huynh Huynh  
College of Education  
Univ. of South Carolina  
Columbia, SC 29208

Dr. Martin J. Ippel  
Center for the Study of  
Education and Instruction  
Leiden University  
P. O. Box 9535  
2300 RB Leiden  
THE NETHERLANDS

Dr. Robert Jannarone  
Elec. and Computer Eng. Dept.  
University of South Carolina  
Columbia, SC 29208

Dr. Kumar Joag-dev  
University of Illinois  
Department of Statistics  
101 Illini Hall  
725 South Wright Street  
Champaign, IL 61820

Professor Douglas H. Jones  
Graduate School of Management  
Rutgers, The State University  
of New Jersey  
Newark, NJ 07102

Dr. Brian Junker  
Carnegie-Mellon University  
Department of Statistics  
Pittsburgh, PA 15213

Dr. Marcel Just  
Carnegie-Mellon University  
Department of Psychology  
Schenley Park  
Pittsburgh, PA 15213

Dr. J. L. Kaiwi  
Code 442/JK  
Naval Ocean Systems Center  
San Diego, CA 92152-5000

Dr. Michael Kaplan  
Office of Basic Research  
U.S. Army Research Institute  
5001 Eisenhower Avenue  
Alexandria, VA 22333-5600

Dr. Jeremy Kilpatrick  
Department of  
Mathematics Education  
105 Aderhold Hall  
University of Georgia  
Athens, GA 30602

Ms. Hae-Rim Kim  
University of Illinois  
Department of Statistics  
101 Illini Hall  
725 South Wright St.  
Champaign, IL 61820

Dr. Jwa-keun Kim  
Department of Psychology  
Middle Tennessee State  
University  
Murfreesboro, TN 37132

Dr. Sung-Hoon Kim  
KEDI  
92-6 Umyeong-Dong  
Seochbo-Gu  
Seoul  
SOUTH KOREA

Dr. G. Gage Kingsbury  
Portland Public Schools  
Research and Evaluation Department  
501 North Dixon Street  
P. O. Box 3107  
Portland, OR 97209-3107

Dr. William Koch  
Box 7246, Meas. and Eval. Ctr.  
University of Texas-Austin  
Austin, TX 78703

Dr. James Kraetz  
Computer-based Education  
Research Laboratory  
University of Illinois  
Urbana, IL 61801

Dr. Patrick Kyttonen  
AFHRL/MOEL  
Brooks AFB, TX 78235

Ms. Carolyn Laney  
1515 Spencerville Road  
Spencerville, MD 20868

Richard Lanierman  
Commandant (G-PWP)  
US Coast Guard  
2100 Second St., SW  
Washington, DC 20593-0001

Dr. Michael Levine  
Educational Psychology  
210 Education Bldg.  
1310 South Sixth Street  
University of IL at  
Urbana-Champaign  
Champaign, IL 61820-6990

Dr. Charles Lewis  
Educational Testing Service  
Princeton, NJ 08541-0001

Mr. Hsin-hung Li  
University of Illinois  
Department of Statistics  
101 Illini Hall  
725 South Wright St.  
Champaign, IL 61820

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Naval Training Systems Center  
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Dr. Marcia C. Linn  
Graduate School  
of Education, EMST  
Tolman Hall  
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Berkeley, CA 94720

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Campus Box 249  
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Dr. George B. Macready  
Department of Measurement  
Statistics & Evaluation  
College of Education  
University of Maryland  
College Park, MD 20742

Dr. Evans Mandes  
George Mason University  
4400 University Drive  
Fairfax, VA 22030

Dr. Paul Mayberry  
Center for Naval Analysis  
4401 Ford Avenue  
P.O. Box 16268  
Alexandria, VA 22302-0268

Dr. James R. McBride  
HumRRO  
6430 Elmhurst Drive  
San Diego, CA 92120

Mr. Christopher McCusker  
University of Illinois  
Department of Psychology  
603 E. Daniel St.  
Champaign, IL 61820

Dr. Robert McKinley  
Educational Testing Service  
Princeton, NJ 08541

Dr. Joseph McLachlan  
Navy Personnel Research  
and Development Center  
Code 14  
San Diego, CA 92152-6800

Alan Mead  
c/o Dr. Michael Levine  
Educational Psychology  
210 Education Bldg.  
University of Illinois  
Champaign, IL 61801

Dr. Timothy Miller  
ACT  
P. O. Box 168  
Iowa City, IA 52243

Dr. Robert Maley  
Educational Testing Service  
Princeton, NJ 08541

Dr. Ivo Molenaar  
Faculteit Sociale Wetenschappen  
Rijksuniversiteit Groningen  
Grote Kruisstraat 2/1  
9712 TS Groningen  
The NETHERLANDS

Dr. E. Muraki  
Educational Testing Service  
Rosedale Road  
Princeton, NJ 08541

Dr. Ratna Nandakumar  
Educational Studies  
Willard Hall, Room 213E  
University of Delaware  
Newark, DE 19716

Academic Progs. & Research Branch  
Naval Technical Training Command  
Code N-62  
NAS Memphis (75)  
Millington, TN 38854

Dr. W. Alan Nicewander  
University of Oklahoma  
Department of Psychology  
Norman, OK 73071

Head, Personnel Systems Department  
NPRDC (Code 12)  
San Diego, CA 92152-6800

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Special Assistant for Research  
Management  
Chief of Naval Personnel (PERS-OLIT)  
Department of the Navy  
Washington, DC 20350-2000

Dr. Judith Orasanu  
Mail Stop 239-1  
NASA Ames Research Center  
Moffett Field, CA 94035

Dr. Peter J. Pashley  
Educational Testing Service  
Rosedale Road  
Princeton, NJ 08541

Wayne M. Patience  
American Council on Education  
GED Testing Service, Suite 20  
One Dupont Circle, NW  
Washington, DC 20036

Dept. of Administrative Sciences  
Code 54  
Naval Postgraduate School  
Monterey, CA 93943-5026

Dr. Peter Pirolli  
School of Education  
University of California  
Berkeley, CA 94720

Dr. Mark D. Reckase  
ACT  
P. O. Box 168  
Iowa City, IA 52243

Mr. Steve Reise  
Department of Psychology  
University of California  
Riverside, CA 92521

Mr. Louis Roussos  
University of Illinois  
Department of Statistics  
101 Illini Hall  
725 South Wright St.  
Champaign, IL 61820

Dr. Donald Rubin  
Statistics Department  
Science Center, Room 608  
1 Oxford Street  
Harvard University  
Cambridge, MA 02138

Dr. Fumiko Samejima  
Department of Psychology  
University of Tennessee  
310B Austin Peay Bldg.  
Knoxville, TN 37966-0900

Dr. Mary Schrauz  
4100 Parkside  
Carlsbad, CA 92008

Mr. Robert Semmes  
N218 Elliott Hall  
Department of Psychology  
University of Minnesota  
Minneapolis, MN 55455-0344

Dr. Valerie L. Stalín  
Department of Industrial  
Engineering  
State University of New York  
342 Lawrence D. Bell Hall  
Buffalo, NY 14260

Mr. Richard J. Shavelson  
Graduate School of Education  
University of California  
Santa Barbara, CA 93106

Ms. Kathleen Sheehan  
Educational Testing Service  
Princeton, NJ 08541

Dr. Kazuo Shigematsu  
7-9-24 Kugenuma-Kaigan  
Fujisawa 251  
JAPAN

Dr. Randall Shumaker  
Naval Research Laboratory  
Code 5500  
4555 Overlook Avenue, S.W.  
Washington, DC 20375-5000

Dr. Judy Spray  
ACT  
P.O. Box 168  
Iowa City, IA 52243

Dr. Martha Stocking  
Educational Testing Service  
Princeton, NJ 08541

Dr. William Stout  
University of Illinois  
Department of Statistics  
101 Illini Hall  
725 South Wright St.  
Champaign, IL 61820

Dr. Kikumi Tatsuoka  
Educational Testing Service  
Mail Stop 03-T  
Princeton, NJ 08541

Dr. David Thissen  
Psychometric Laboratory  
CB# 3270, Davie Hall  
University of North Carolina  
Chapel Hill, NC 27599-3270

Mr. Thomas J. Thomas  
Federal Express Corporation  
Human Resource Development  
3035 Director Row, Suite 501  
Memphis, TN 38131

Mr. Gary Thomasson  
University of Illinois  
Educational Psychology  
Champaign, IL 61820

Dr. Howard Wainer  
Educational Testing Service  
Princeton, NJ 08541

Elizabeth Wald  
Office of Naval Technology  
Code 227  
800 North Quincy Street  
Arlington, VA 22217-5000

Dr. Michael T. Walter  
University of  
Wisconsin-Milwaukee  
Educational Psychology Dept.  
Box 413  
Milwaukee, WI 53201

Dr. Ming-Mei Wang  
Educational Testing Service  
Mail Stop 03-T  
Princeton, NJ 08541

Dr. Thomas A. Warm  
FAA Academy  
P.O. Box 25082  
Oklahoma City, OK 73125

Dr. David J. Weiss  
N660 Elliott Hall  
University of Minnesota  
75 E. River Road  
Minneapolis, MN 55455-0344

Dr. Douglas Wetzel  
Code 15  
Navy Personnel R&D Center  
San Diego, CA 92152-6800

German Military  
Representative  
Personalstammamt  
Koelner Str. 262  
D-5000 Koeln 90  
WEST GERMANY

Dr. David Wiley  
School of Education  
and Social Policy  
Northwestern University  
Evanston, IL 60208

Dr. Bruce Williams  
Department of Educational  
Psychology  
University of Illinois  
Urbana, IL 61801

Dr. Mark Wilson  
School of Education  
University of California  
Berkeley, CA 94720

Dr. Eugene Winograd  
Department of Psychology  
Emory University  
Atlanta, GA 30322

Dr. Martin F. Wiskoff  
PIRSEREC  
90 Pacific St., Suite 4556  
Monterey, CA 93940

Mr. John H. Wolfe  
Navy Personnel R&D Center  
San Diego, CA 92152-6800

Dr. Kentaro Yamamoto  
63-07  
Educational Testing Service  
Rosedale Road  
Princeton, NJ 08541

Ms. Duanli Yan  
Educational Testing Service  
Princeton, NJ 08541

Dr. Wendy Yen  
CTB McGraw Hill  
Del Monte Research Park  
Monterey, CA 93940

Dr. Joseph L. Young  
National Science Foundation  
Room 320  
1800 G Street, N.W.  
Washington, DC 20550